Method of Undetermined Coefficients

Inhomogeneous equation:

$$a_0y + a_1y' + a_2y'' + a_3y^{(3)} + \ldots + a_ny^{(n)} = q$$

where $q \neq 0$.

First solve the homogeneous equation, then guess a particular solution with a few undetermined coefficients:

For $q =:$	guess $y_p =:$
$e^{\alpha x}$	$Ce^{\alpha x}$
$e^{\lambda x}$	$Cx^n e^{\lambda x}$
$\cos x$	$C_1 \cos x + C_2 \sin x$
polynomial	polynomial

The general solution is any particular solution plus the general solution of the homogeneous equation.