4.42

1 4.42, §1 Asked

Solve:

$$\frac{\mathrm{d}y}{\mathrm{d}x} = -(x^2 + 1)y$$
 $y = 1$ at $x = -1$

2 4.42, §2 Solution

$$\frac{\mathrm{d}y}{\mathrm{d}x} = -(x^2 + 1)y$$
 $y = 1$ at $x = -1$



Solve the O.D.E. first:

$$\frac{\mathrm{d}y}{y} = -(x^2 + 1)\,\mathrm{d}x$$

$$\ln|y| = -\frac{1}{3}x^3 - x + C$$

$$y = \pm e^C e^{-\frac{1}{3}x^3 - x}$$

$$y = De^{-\frac{1}{3}x^3 - x}$$



Since the additional condition is y = 1 at x = -1, substitute in y = 1 and x = -1 to get D: $1 = De^{\frac{1}{3}+1}$

So, at any x:

$$y = e^{-\frac{1}{3}x^3 - x - \frac{4}{3}}$$