## FUNCTIONS

$$
\begin{array}{lll}
\sin \left(\frac{\pi}{6}\right)=0.5 & \sin (30)=-0.988 & \text { Radians are default, as they should be! } \\
\sin \left(30^{\circ}\right)=0.5 & \sin (30 \mathrm{deg})=0.5 & \text { Use the measuring cup for the raised circle. }
\end{array}
$$

Open menu Help, item Mathcad Help, and use search to find out how to insert an arcsine.

$$
\begin{array}{llcl}
\exp (2)=7.389 & \mathrm{e}^{2}=7.389 & \text { or the sqaure root } & \\
\ln \left(\mathrm{e}^{2}\right)=2 & \log \left(\mathrm{e}^{2}\right)=0.869 & \log \left(\mathrm{e}^{2}, \mathrm{e}\right)=2 & \text { The } \ln \text { is always base } \mathrm{e} . \\
\ln \left(10^{2}\right)=4.605 & \log \left(10^{2}\right)=2 & \log \left(10^{2}, 10\right)=2 & \text { Base } 10 \text { is default for log. }
\end{array}
$$

For a square root use $\backslash: \quad \sqrt{9}=3$
For another root, use Ctrl $+\backslash: \quad \sqrt[3]{27}=3$
You can define your own functions much like you define your own variables:

$$
\operatorname{sqr}(x):=x^{2} \quad \operatorname{sqr}(2)=4 \quad \operatorname{sqr}(3)=9
$$

You can also define piecewise functions. How about a function that is a parabola for negative $x$, but linear for positive $x$ ?

$$
\operatorname{parlin}(\mathrm{x}):=\operatorname{if}\left(\mathrm{x}<0, \mathrm{x}^{2}, \mathrm{x}\right)
$$

$$
\operatorname{parlin}(-2)=4 \quad \operatorname{parlin}(-1)=1 \quad \operatorname{parlin}(1)=1 \quad \operatorname{parlin}(2)=2
$$

You could cap off the large values at negative $x$ at 3 :

$$
\operatorname{parlin}(x):=\text { if }\left(x<0, \text { if }\left(x^{2}<3, x^{2}, 3\right), x\right)
$$

$$
\operatorname{parlin}(-2)=3 \quad \operatorname{parlin}(-1)=1 \quad \operatorname{parlin}(1)=1 \quad \operatorname{parlin}(2)=2
$$

How about capping it off at both sides? Does it need 3 if constructs or is 2 enough? I think you need 3 (without using build in piecewise functions like min and absolute).

You can also define functions that produce strings. Use a double quote to start a string and get out of it using the arrow key:
textsign( x ) := concat("x is ", if $(\mathrm{x}>0$, "positive", "not positive" $)$ )
textsign $(-3)=" x$ is not positive" textsign $(0)=" x$ is not positive" textsign $(2)=" x$ is positive"

## QUICK PLOTS

Simple plots are started by typing @ (Shift 2), or using the graph toolbar. After typing @, fill in the axes placeholders appropriately. Right-click the graph and select Properties and Format to add a border and title:



Use the Format menu to enable a second $y$-axis if needed:


Without the second y-axis, you would either not see the logarithm or the exponential properly.

For functions of two variables, you can either do a contour plot or a three-dimensional surface plot. Note: I had to set the monitor to 16 bit to get the 3D graphs to work. Alternatively, create a Mathcad desltop item, right-click it, select Compatibility, and disable desktop composition.
$\mathrm{f}(\mathrm{x}, \mathrm{y}):=\mathrm{x}^{2}-\mathrm{y}^{2} \quad$ The function we will plot.


I had to change the axes in Properties, Quickplot Data, to get a decent graph. I also had to grab an axis and move it around.

Note: to do plots of space curves in three-dimensional space, use CreateSpace, then select a scatter plot from the menu Insert / Graph or graph toolbar. Then use the right-click Properties menu to change points into lines. This is not said in the Mathcad help.

## RANGE VARIABLES

A range variable is a list of equally spaced numbers, like say $1.5,2,2.5, \ldots, 4$. To create a range variable with those values, type 1.5,2;4 (note that the semi-colon contains a comma and a point:

cens a country have $0.5,1,1.5,2$, and 2.5 cm . You want to compare coin volumes in cubic mm for coin thicknesses 1 mm and 0.7 mm using range variables.

First look under Help, Reference Tables, and find the formula for the volume of a right circular cylinder. Define a function that way:
$\mathrm{V}_{\mathrm{cyl}}(\mathrm{r}, \mathrm{h}):=\pi \cdot \mathrm{r}^{2} \cdot \mathrm{~h} \quad \mathrm{~V}_{\mathrm{cyl}}=f($ any 1, any 2$) \rightarrow$ any $1 \wedge 2 \cdot$ any 2
Define the coin thicknesses and a range variable with the diameter values D :

| $\mathrm{t}_{1}:=1 \mathrm{~mm}$ | $\mathrm{t}_{2}:=0.7 \mathrm{~mm}$ | $\mathrm{D}:=0.5 \mathrm{~cm}, 1 \mathrm{~cm} . .2 .5 \mathrm{~cm}$ |
| :--- | :--- | :--- | | $\mathrm{t}_{1}=1 \cdot \mathrm{~mm}$ | $\mathrm{t}_{2}=0.7 \cdot \mathrm{~mm}$ |
| :--- | :--- | $\mathrm{D}=$| You must specify the units on |
| :--- | :--- |
| each member of the range variable |

$\mathrm{t}_{1}=1 \cdot \mathrm{~mm} \quad \mathrm{t}_{2}=0.7 \cdot \mathrm{~mm} \quad \mathrm{D}=$
each member of the range variable

| 0.5 |
| ---: |
| 1 |
| 1.5 |
| 2 |
| 2 |
| 2.5 |

Now we can evaluate the coin volumes:
$\mathrm{V}_{\text {cyl }}\left(\frac{\mathrm{D}}{2}, \mathrm{t}_{1}\right)=\quad \mathrm{V}_{\text {cyl }}\left(\frac{\mathrm{D}}{2}, \mathrm{t}_{2}\right)=\quad \begin{aligned} & \text { Do not try to assign these to a range } \\ & \text { variable }\end{aligned}$

| 19.635 | .mm ${ }^{3}$ | 13.744 |
| :---: | :---: | :---: |
| 78.54 |  | 54.978 |
| 176.715 |  | 123.7 |
| 314.159 |  | 219.911 |
| 490.874 |  | 343.612 |

variable.
I had some problems with Mathcad converting range variables to matrices without my permission. Buggy, buggy.

People pay $\$ 1,600.00$ for that?

Let's plot this!


Note that Mathcad does not add units to the numbers on the axes; they are nondimensional numbers. Therefore, to get Mathcad to list the numbers that multiply the centimeters in D , you must divide D by cm . And it goes similarly for $V_{\text {cyl }}$.

Use the right-click Format menu to put in the border and title, and to show the trace as symbols instead of a line.

To make a presentation-quality graph, you want to hide the trace arguments, add explicit $x$ and $y$ labels, and add a legend. Do that with the right-click Format menu.


To put the superscript 3 in the label of the y axis, use the Microsoft character map program found in the Start Menu / Accessories / System Tools.

Note: If you are plotting some function, and Mathcad does not put enough points in the curve (buggy, buggy), use a range variable as independent variable. That allows you to specify the plot points yourself.

