## Second Law of Thermodynamics

As an introduction to the Second Law of Thermodynamics, recall the First Law. The First Law is a statement of conservation of energy expressed for a process as:

$$\Delta U = Q_{12} - W_{12}$$

and for a cycle as:

$$\sum Q = \sum W$$

Consider some limitations of the First Law. Take a piston-cylinder example such as the spark ignition (Otto cycle) automotive cycle.



For the cycle we have:

$$\sum Q = Q_{in} - Q_{out} = \sum W = -W_{in} + W_{out} = W_{net}$$

The efficiency of the energy conversion, from  $Q_{in}$  to  $W_{net}$  is given as

$$\eta = \frac{W_{net}}{Q_{in}} = \frac{Q_{in} - Q_{out}}{Q_{in}} = 1 - \frac{Q_{out}}{Q_{in}}$$

From the expression for the efficiency there is no indication to the limits on the relative values of Q's. For example,  $Q_{out}$  could be as small as we please without violating the energy balance and thus approach a 100% efficiency of conversion from heat to work. Thus the First law does not limit the extent of the conversion of one form of energy to another.

The first law also does not indicate if a particular process or cycle is feasible as long as it does not violate the first law.

The first law does not indicate the direction of a process. For example, a block left on an inclined plane will spontaneously slide down (in a gravitational field and with negligible friction). However a block at the bottom of the inclined plane will not spontaneously move up.



### Aspects of the Second Law.

The second law of thermodynamics and deductions from it will provide a means for

- Predicting the direction of processes
- Establishing conditions of equilibrium
- Determining the best theoretical performance of cycles, engines, and other devices
- Defining a temperature scale independent of the properties of thermodynamic substance

# **Statements of the Second Law of Thermodynamics**

Clausius Statement: Application: Refrigerators and Heat Pumps

It is impossible for any system to operate in such a way that the sole result would be an energy transfer by heat from a cooler to a hotter body.



Low Temperature Reservoir, T<sub>L</sub>

Kelvin-Plank Statement - Application: Heat Engines

# It is impossible for any system to operate in a thermodynamic cycle and deliver a net amount of work to its surroundings while receiving energy by heat transfer from a single thermal reservoir.



 $Q_{\rm L}$ 

Low Temperature Reservoir, T<sub>L</sub>

The Clausius and the Kelvin-Plank statements are equivalent.

The equivalence is demonstrated by showing that the violation of one statement implies the violation of the other.

**Second Law Corollaries** 

It is impossible to construct an engine, operating between two given thermal reservoirs, that is more efficient than a reversible engine operating between the same two reservoirs.



#### Proof:

- 1) Let any heat engine I and a reversible engine R operate between the high and low temperature reservoirs  $T_H$  and  $T_L$ .
- 2) Assume the statement above is false, i.e. assume

$$\eta_{\rm I} > \eta_{\rm R}$$

3) Operate the engines such that

$$Q_{\rm IH} = Q_{\rm RH} = Q_{\rm H}$$

4) By definition:

$$\eta = \frac{Wnet}{Qin}$$
 and  $\eta_{I} = \frac{WI}{QH}$ ,  $\eta_{R} = \frac{WR}{QH}$ 

by assumption:

$$\eta_{\rm I} = \frac{WI}{QH} > \eta_{\rm R} = \frac{WR}{QH},$$

hence: WI > WR

# 5) Reverse the reversible engine:



6) Since WI > WR, take part of WI and supply WR.



7) Use QHR to supply QHI, note that QHI = QHR = QH

High Temperature Reservoir,  $T_{H}$ 



8) Take the two engines as a single system.



9) Note that now we now have a single engine (system) which exchanges heat with a single reservoir  $T_L$  and produces net work  $W_I - W_R$ . This is a direct violation of the second law of thermodynamics.



10) CONCLUSION: It is impossible to construct an engine that operates between two given reservoirs and is more efficient than a reversible engine operating between the same two reservoirs, i.e.

$$\eta_{I} \leq \eta_{R}$$

All reversible engines operating between the same temperature limits have the same efficiency.

Proof:

1) Take two reversible engines R1 and R2



- 2) Follow proof as above. Assume  $\eta_{R1} > \eta_{R2}$
- 3) Reverse reversible engine R2 and let QH2 = QH1 = QH
- 4) This will lead to the conclusion that  $\eta_{R1} \leq \eta_{R2}$
- 5) Next assume  $\eta_{R2} > \eta_{R1}$
- 6) Reverse reversible engine R1 and let QH1 = QH2 = QH
- 7) This will lead to the conclusion that  $\eta_{R2} \leq \eta_{R1}$
- 8) There is a contradiction unless  $\eta_{R1} = \eta_{R2}$

NOTE: In the above no restrictions were placed upon the type of engine or system to be used or upon the details of the operation, hence the results are completely general.