Intake and Exhaust Valve Flows

• The flow rate through a valve can be given by using the isentropic flow relation and mass conservation:

$$\dot{m}_{is} = \rho A_{\nu} U = \rho A_{\nu} \left\{ 2 \frac{\gamma}{\gamma - 1} \frac{P_o}{\rho_o} \left(1 - \left(\frac{P}{P_o} \right)^{(\gamma - 1)/\gamma} \right) \right\}^{1/2},$$

where $P_o \& \rho_o$ are stagnation pressure and density, respectively, P=valve static pressure, A_v is a representative area of the valve. \Rightarrow The actual mass flow can be related to the ideal isentropic mass flow by: $\dot{m}_{actaul} = C_f \dot{m}_{is}$, where C_f is a valve flow coefficient and it is the ratio of an effective flow area (due to flow contraction or separation) to the valve seat area (that is when $A_v = \frac{\pi}{4}D^2$). $C_f = A_f / A_v = A_f / \left(\frac{\pi}{4}D^2\right)$ and $C_f < 1$ to account for the non-isentopic

nature of the flow.

Choked Condition

 \Rightarrow Choked flow occur when the flow speed at the throat reaches local speed of sound. As a result, the pressure ratio reaches a critical valve as

$$\left(\frac{P_{o}}{P_{throat}}\right)_{cr} = \left(\frac{\gamma+1}{2}\right)^{\gamma/(\gamma-1)}$$

The choked mass flow rate is then

$$\dot{m}_{\rm choked} = \rho_o C_f A_v a_o \left(\frac{2}{\gamma+1}\right)^{(\gamma+1)/2(\gamma-1)} = \rho_o A_f a_o \left(\frac{2}{\gamma+1}\right)^{(\gamma+1)/2(\gamma-1)},$$

where a_0 is the stagnation speed of sound and $A_f = C_f A_v$.

 \Rightarrow Note: If the representative area is the valve curtain area, the flow coefficient is called the discharge coefficient:

$$A_f = C_D A_v = C_D (\pi DL).$$

Valve Flow Pattern

 \succ Due to the strong viscous effect at the valve, several types of flow patterns can exist at different valve lift positions.

(a) Low lift: flow reattachment on both sides and jet fills the gap.

(b) Intermediate lift: one side reattach while the other side separates from the valve and jet partially fills the gap.(c) High lift: both sides separate to form a free jet.





Volumetric Efficiency and Mach Index

We can define the mass inducted during the valve opening period as:

$$\mathbf{m}_{i} = \frac{\Delta t}{\Delta \theta} \int_{\theta_{io}}^{\theta_{ic}} \dot{m} d\theta = \frac{1}{\omega} \int_{\theta_{io}}^{\theta_{ic}} \dot{m} d\theta$$

where θ_{io} and θ_{ic} are crank angles at which the intake value opens and closes, respectively.

Define an averaged effective intake flow area \overline{A}_{f} such that

$$\overline{A}_{f} = \frac{1}{\theta_{ic}} - \theta_{io} \int_{\theta_{io}}^{\theta_{ic}} A_{f} d\theta.$$

One can show that the choked volumetric efficiency

can be expressed as

$$\eta_{\rm v} = \frac{m_i}{\rho_i V_d} = \left(\frac{2}{\gamma+1}\right)^{(\gamma+1)/2(\gamma-1)} \frac{\overline{A}_{\rm f} a_i}{\omega V_d} (\theta_{\rm ic} - \theta_{\rm io}).$$

Volumetric Efficiency and Mach Index

Introduce Mach index Z as

$$Z = \frac{\frac{\pi}{4}b^2 \overline{U}_P}{\overline{A}_f a_i}$$
. Z is clearly related to some reference

Mach number
$$\overline{U}_P/a_i$$
.

Using γ =1.4, the volumetric efficiency for a choked flow is

$$(\eta_{v})_{choked} = 0.58 \left(\frac{\theta_{ic} - \theta_{io}}{\pi} \right) \frac{1}{Z}.$$

For an engine that $\left(\frac{\theta_{ic} - \theta_{io}}{\pi} \right) = 1.3, \ (\eta_{v})_{choked} = \frac{0.75}{Z}$

This represents an upper limit for the volumetric efficiency.

Volumetric Efficiency and Mach Index



 η_{v}

Not as vulnerable to choking —

• Z>0.6, flow choked at the valve.

• $A_f > 1.3b^2(U_p/a_i)$

• Also note that, the intake and exhaust area can be related through their local speed of sound as

$$\frac{A_e}{A_i} \approx \frac{a_i}{a_e} = \left(\frac{T_i}{T_e}\right)^{1/2}.$$

Exhaust valves can be smaller than intake valves since exhaust gas has a

higher local speed of sound.

Effect on Volumetric Efficiency



Piston speed

* At high engine speeds, the inertia of the intake gas can assist to ram more gas into the cylinder, volumetric efficiency is increased by delaying the inlet valve closing ** On the other hand, at the low engine speeds, backflow can occur since the cylinder pressure increases as a result of upward piston movement, thus decreasing the volumetric efficiency.