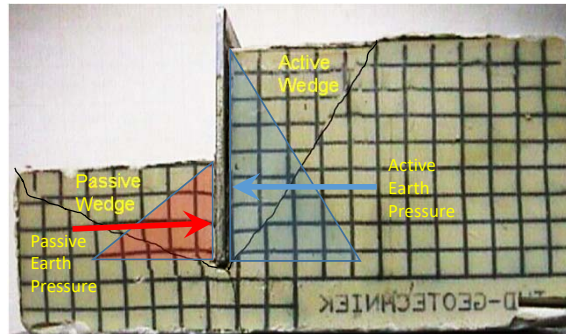
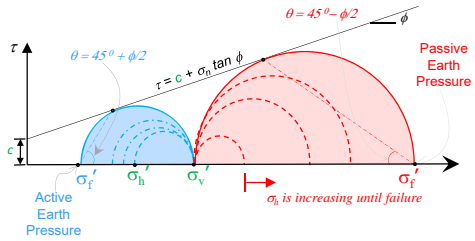
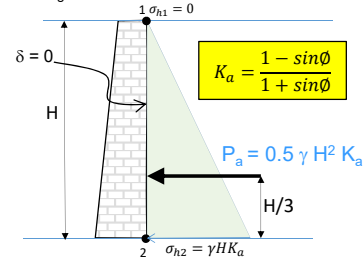


# Rankine's Earth Pressure Method for (c-φ) Soil

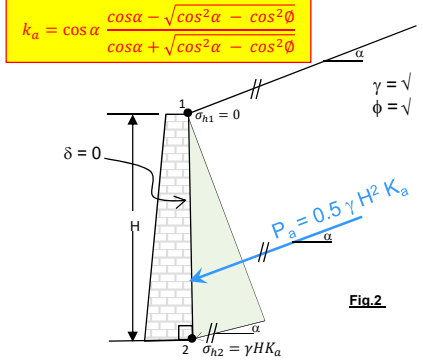
Rankine's Active and Passive Earth Pressure in (c-φ) Soil



Rankine's Active Earth Pressure in (φ) Soil



Rankine's Active Earth Pressure in (φ) Soil with inclined backfill



## Active Earth Pressure

$$\sigma'_f = \sigma'_v \tan^2 \left( 45^\circ - \frac{\phi}{2} \right) + 2c \tan \left( 45^\circ - \frac{\phi}{2} \right)$$

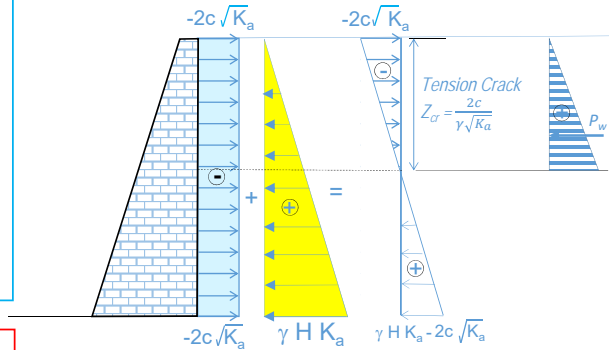
Or

$$\sigma'_f = \sigma'_v K_a - 2c \sqrt{K_a}$$

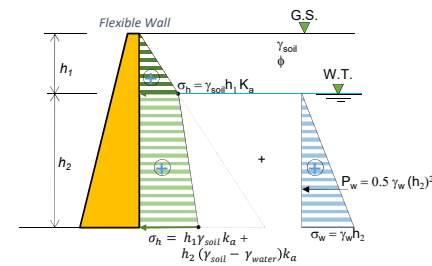
$$K_a = \tan^2 \left( 45^\circ - \frac{\phi}{2} \right) = \frac{1 - \sin \phi}{1 + \sin \phi}$$

Coefficient of active earth pressure

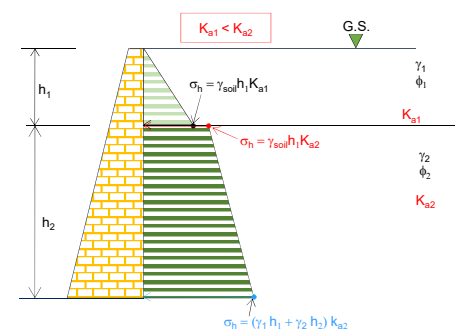
Effect of Cohesion of the Rankine's Active and Passive Earth Pressure



Rankine's Active Earth Pressure in f- Soil & Water Table



Effect of Two Soil Layers on Active Earth Pressure



## Passive Earth Pressure

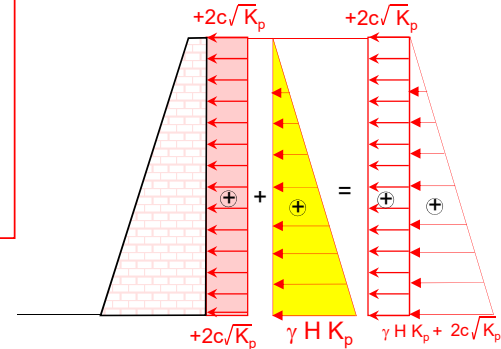
$$\sigma'_f = \sigma'_v \tan^2 \left( 45^\circ + \frac{\phi}{2} \right) + 2c \tan \left( 45^\circ + \frac{\phi}{2} \right)$$

Or

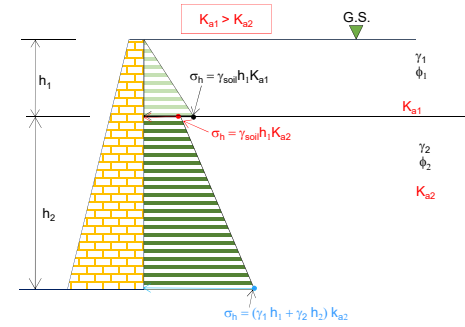
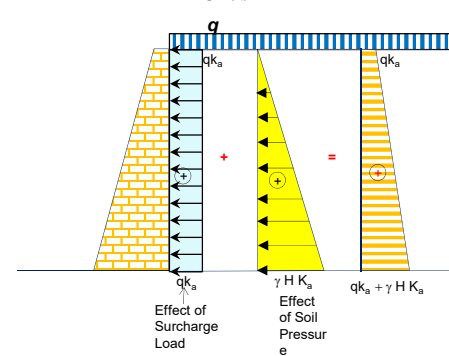
$$\sigma'_f = \sigma'_v K_p + 2c \sqrt{K_p}$$

$$K_p = \tan^2 \left( 45^\circ + \frac{\phi}{2} \right) = \frac{1 + \sin \phi}{1 - \sin \phi}$$

Coefficient of passive earth pressure



Effect of Surcharge (q) Load on Active Earth Pressure



# COULOMB'S WEDGE THEORY

**W** = weight of the soil wedge  
**R** = resultant of the shear and normal forces on the failure surface BC  
**P<sub>a</sub>** = the active force per unit length of the wall. The direction of P<sub>a</sub> is inclined at an angle δ to the normal drawn and the face of the wall that supports the soil  
**δ** = the angle of friction between the soil and the wall

$$W = \gamma \cdot (\text{area of wedge } ABC)$$

From the triangles of forces,

$$\frac{P_a}{\sin(\theta - \phi)} = \frac{W}{\sin(180^\circ - \psi - \theta + \phi)}$$

$$P_a = \frac{W \sin(\theta - \phi)}{\sin(180^\circ - \psi - \theta + \phi)}$$

Substituting for W,

$$P_a = \frac{1}{2} \cdot \frac{\gamma H^2}{\sin^2 \alpha} \cdot \frac{\sin(\theta - \phi)}{\sin(180^\circ - \psi - \theta + \phi)} \cdot \frac{\sin(\theta + \alpha) \cdot \sin(\alpha + \beta)}{\sin(\theta - \beta)}$$

The maximum value of P<sub>a</sub> is obtained by equating the first derivative of P<sub>a</sub> with respect to θ to zero; or

(∂P<sub>a</sub>)/∂θ = 0, and substituting the corresponding value of θ.

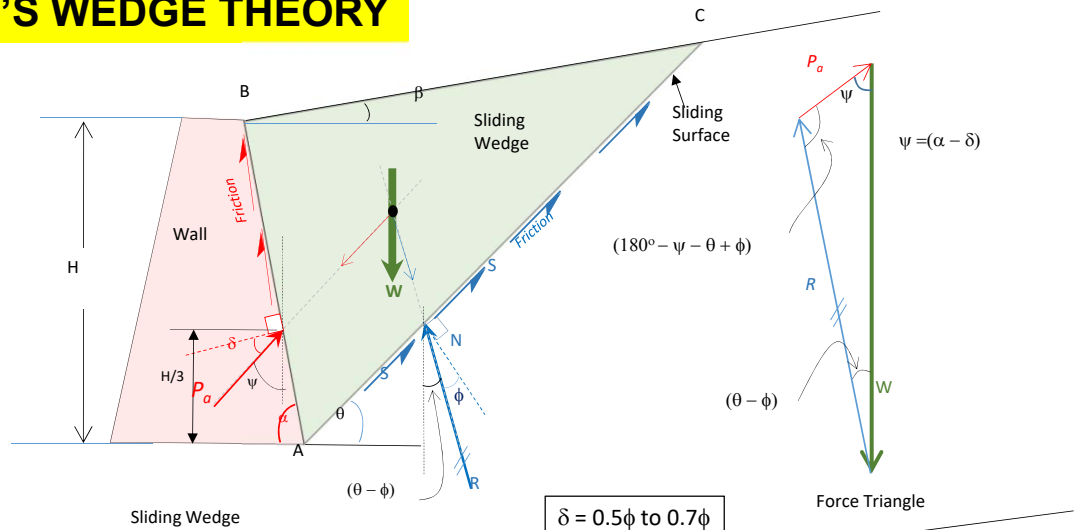
The value of P<sub>a</sub> so obtained is written as

$$P_a = \frac{1}{2} \cdot \gamma H^2 \cdot \frac{\sin^2(\alpha + \phi)}{\sin^2 \alpha \sin(\alpha - \delta) \left[ 1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \beta)}{\sin(\alpha - \delta) \sin(\alpha + \beta)}} \right]^2}$$

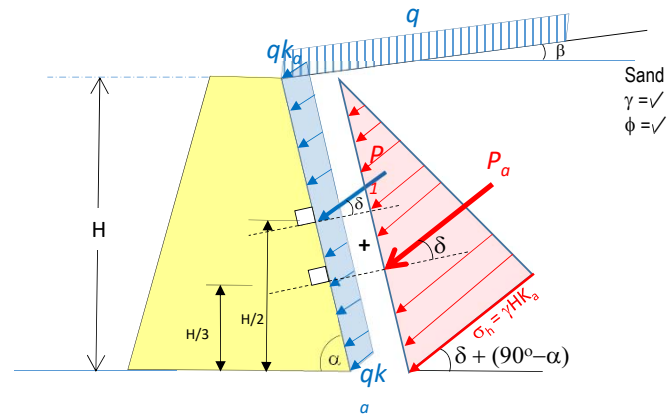
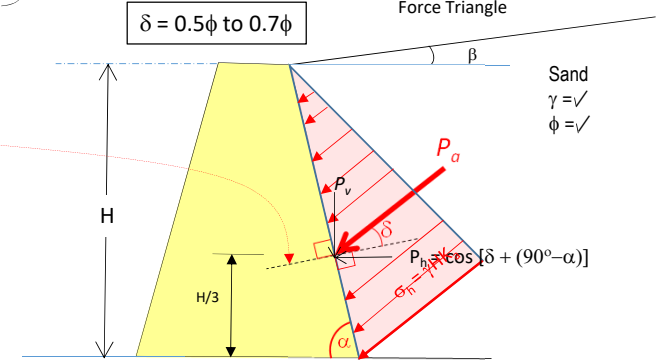
This is usually written as

$$P_a = \frac{1}{2} \cdot \gamma H^2 \cdot K_a$$

Where K<sub>a</sub> being the coefficient of active earth pressure = 
$$\frac{\sin^2(\alpha + \phi)}{\sin^2 \alpha \sin(\alpha - \delta) \left[ 1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \beta)}{\sin(\alpha - \delta) \sin(\alpha + \beta)}} \right]^2}$$



- Draw this perpendicular line first
- Then draw P<sub>a</sub> with an angle = α



# Earth Retaining Walls

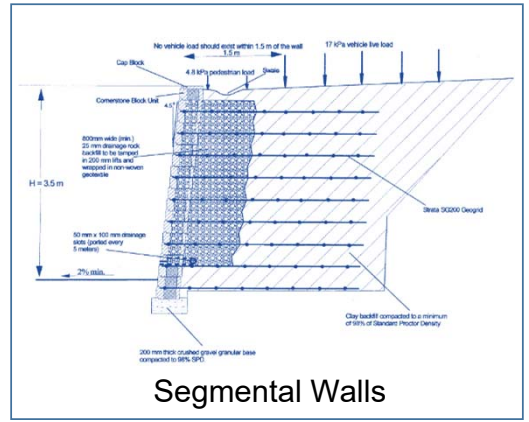
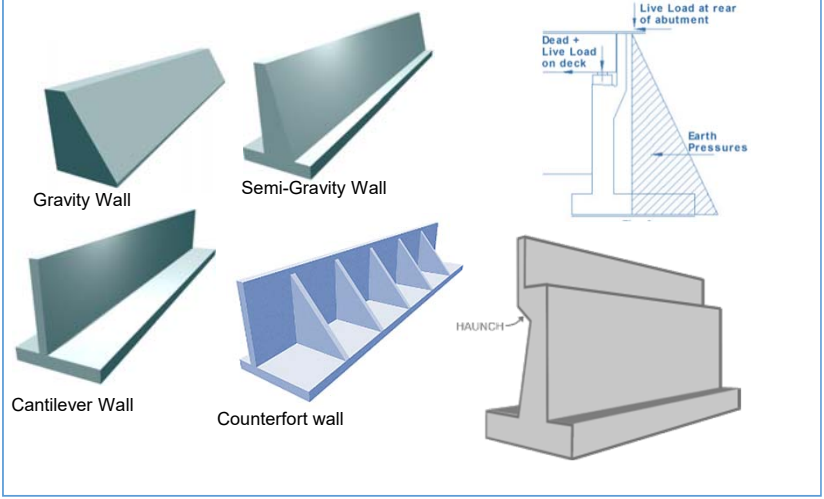




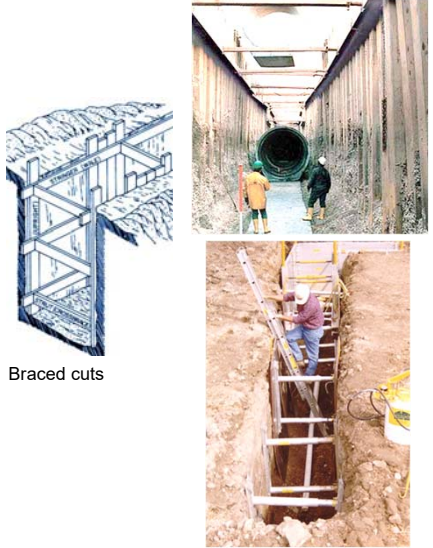
# Design of Retaining Wall

## Types of Earth Retaining Walls

### I- Permanent Walls



### II- Temporary Walls



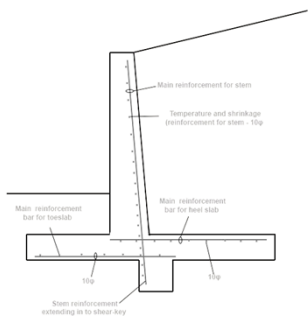
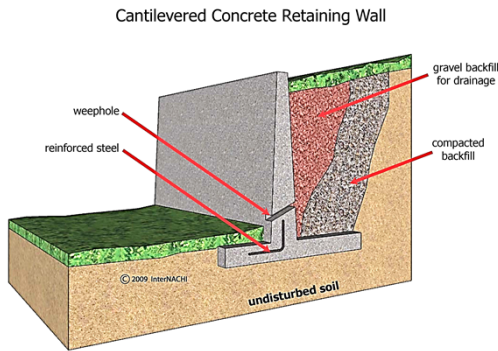
# Design of Retaining Wall

By Kamal Tawfiq, Ph.D., P.E

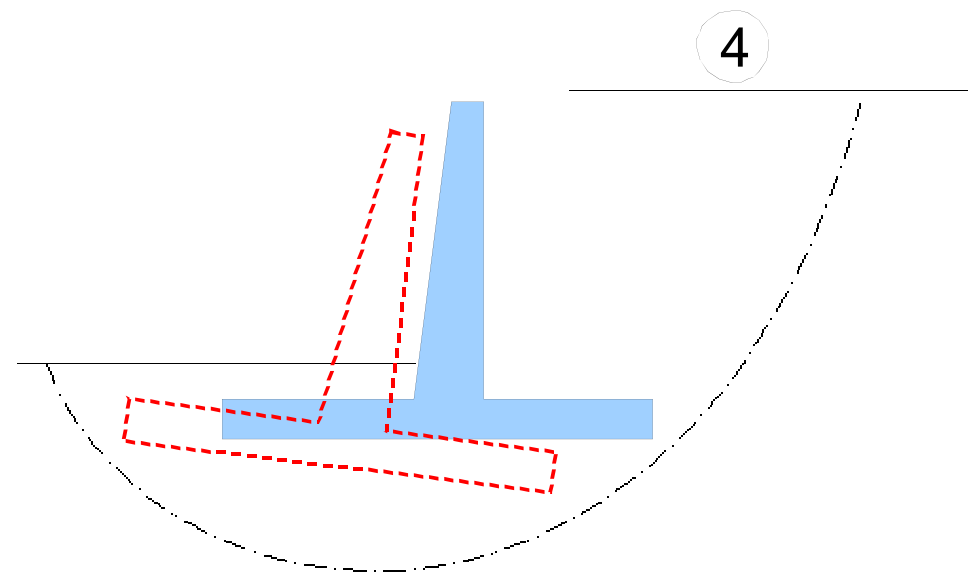
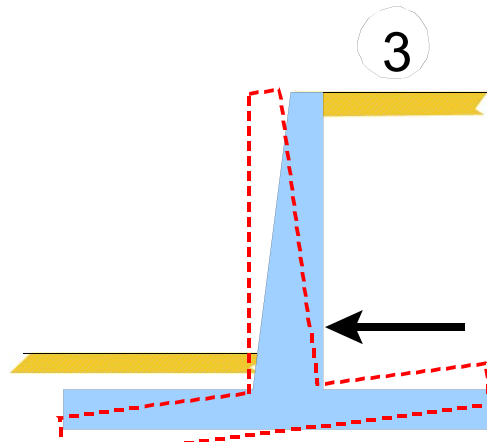
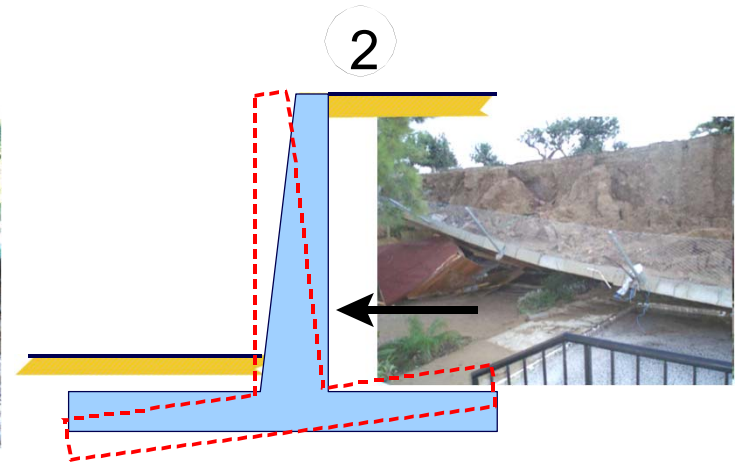
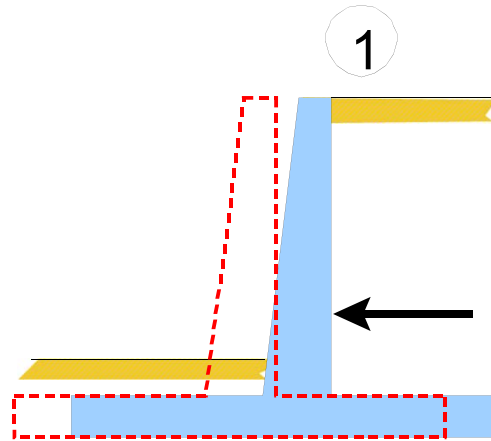
- 1- External Stability
- 2- Internal Stability

## 1. External Stability

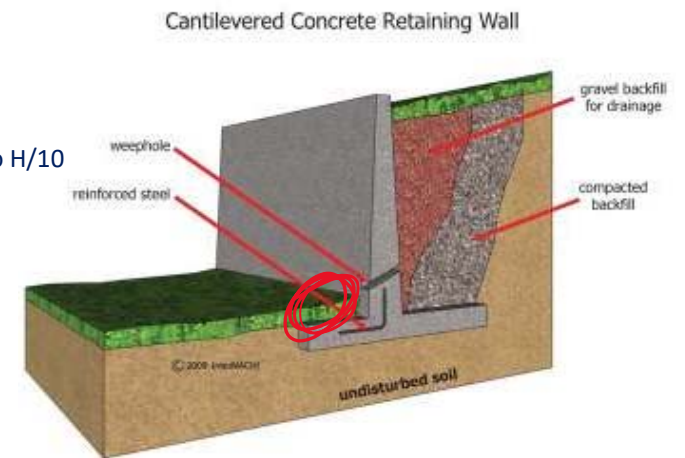
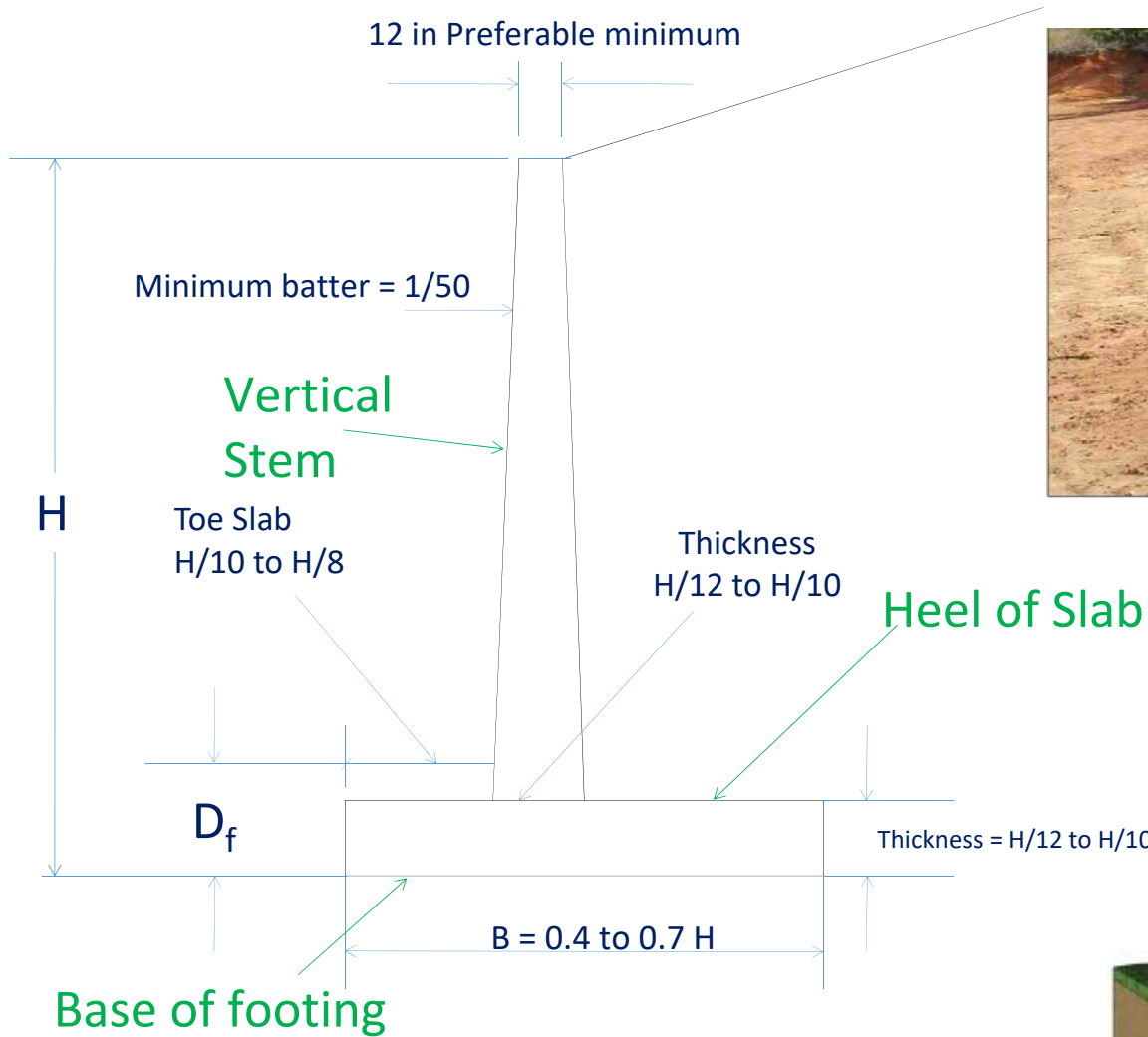
- 1- Sliding
- 2- Overturning
- 3- Settlement
- 4- Overall Failure



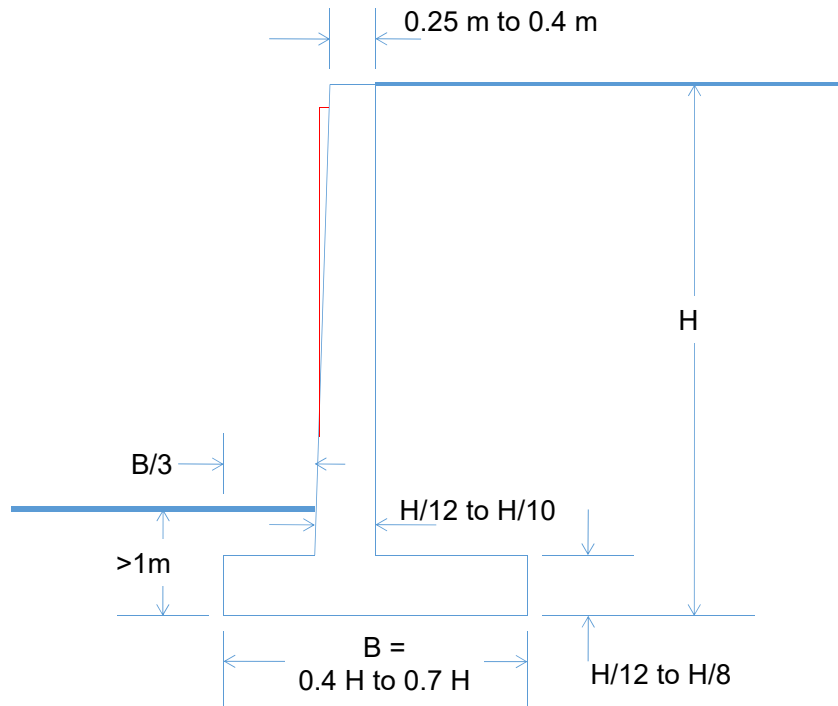
**Internal Stability**  
Steel Reinforcement and Thicknesses



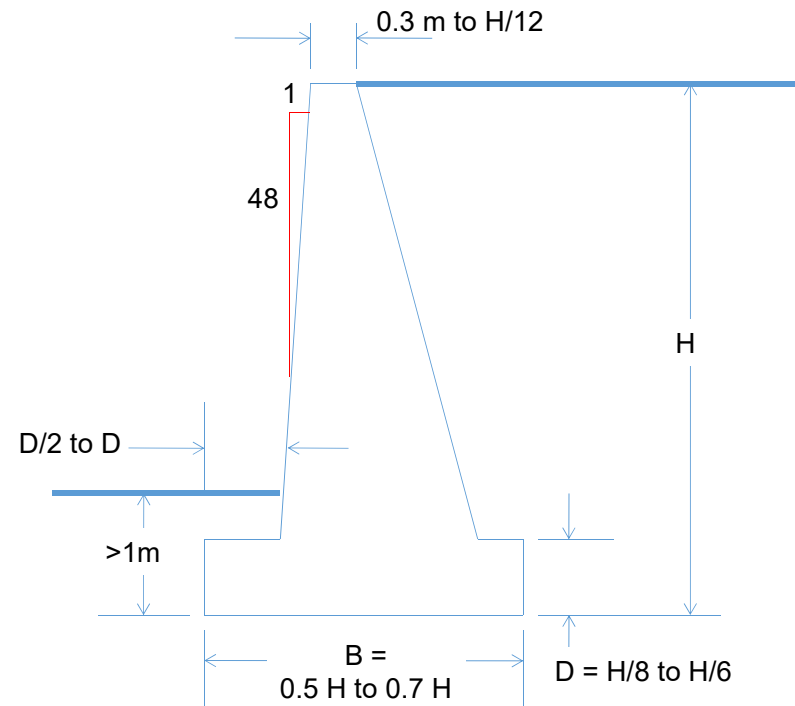
# Common Proportions of Cantilever Wall



## Approximate Dimensions



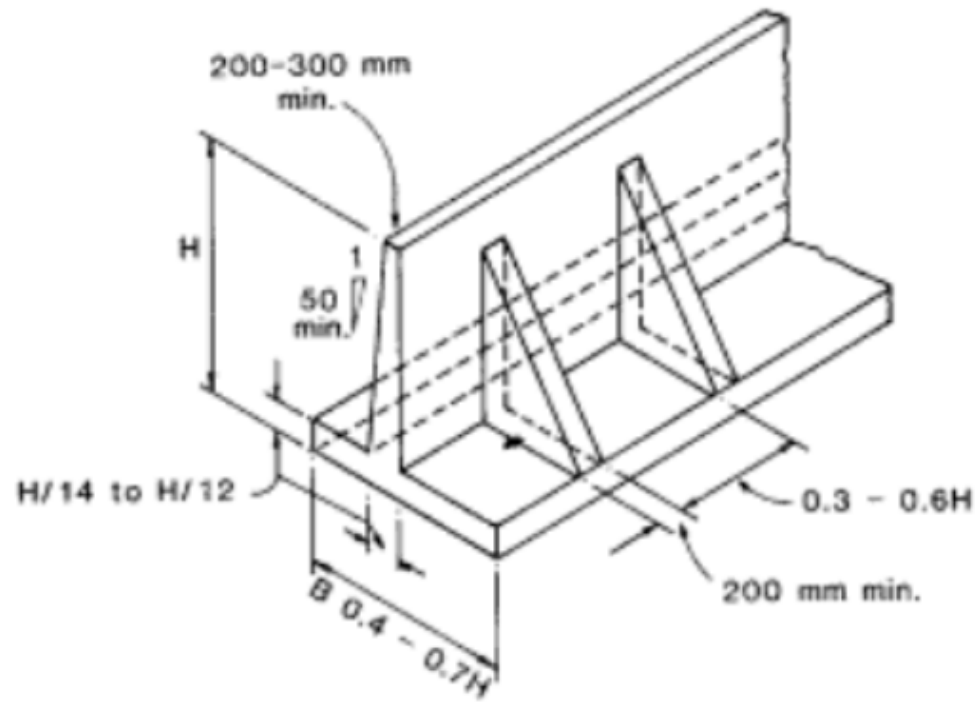
Cantilever Retaining Wall



Gravity Retaining Wall



# Counterfort Retaining Wall





# Internal Stability

**Structural Design**  
Steel Reinforcement  
and Thicknesses } Structural Design

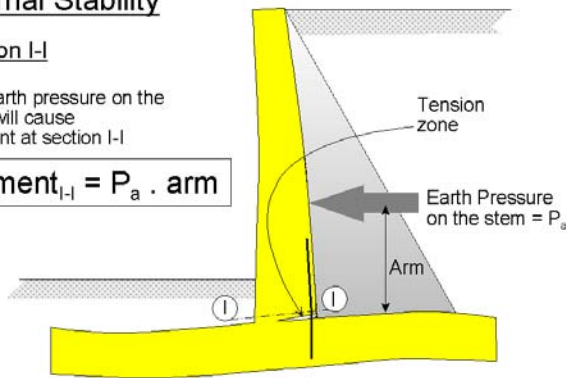
2-

## Internal Stability

### Section I-I

The earth pressure on the stem will cause moment at section I-I

$$\text{Moment}_{I-I} = P_a \cdot \text{arm}$$

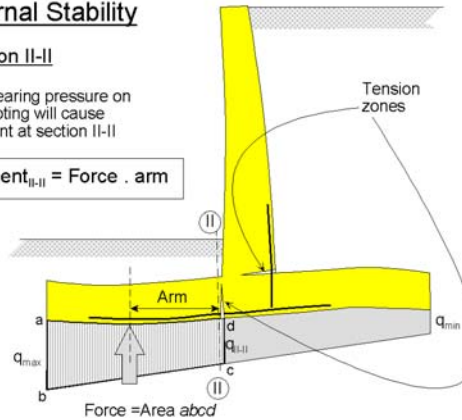


## Internal Stability

### Section II-II

The bearing pressure on the footing will cause moment at section II-II

$$\text{Moment}_{II-II} = \text{Force} \cdot \text{arm}$$

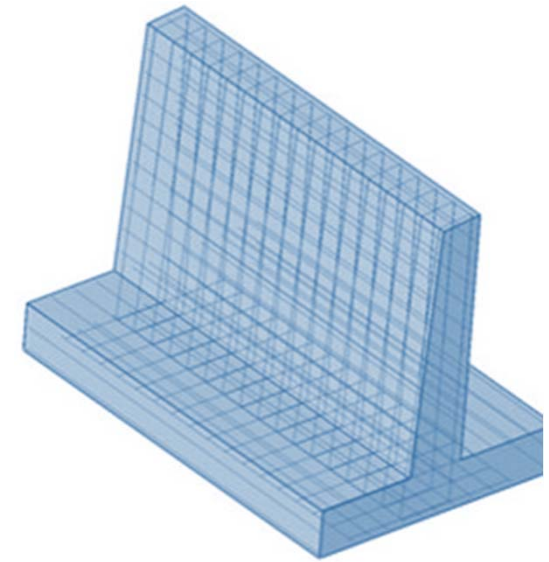
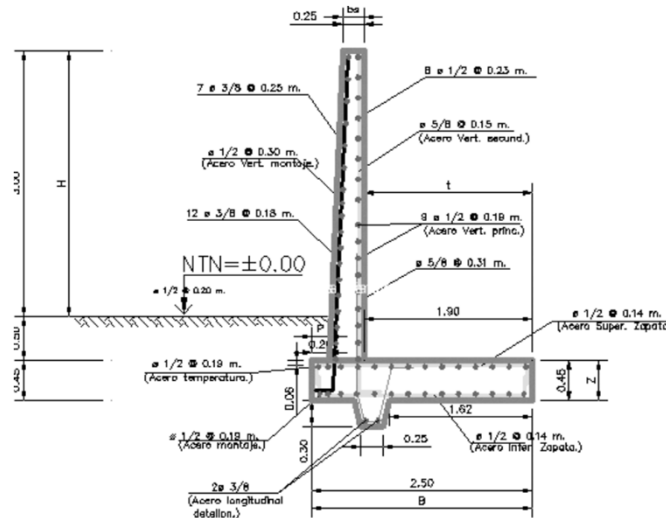
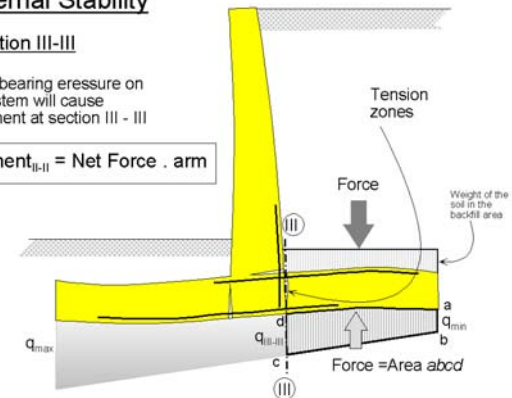


## Internal Stability

### Section III-III

The bearing pressure on the stem will cause moment at section III-III

$$\text{Moment}_{III-III} = \text{Net Force} \cdot \text{arm}$$

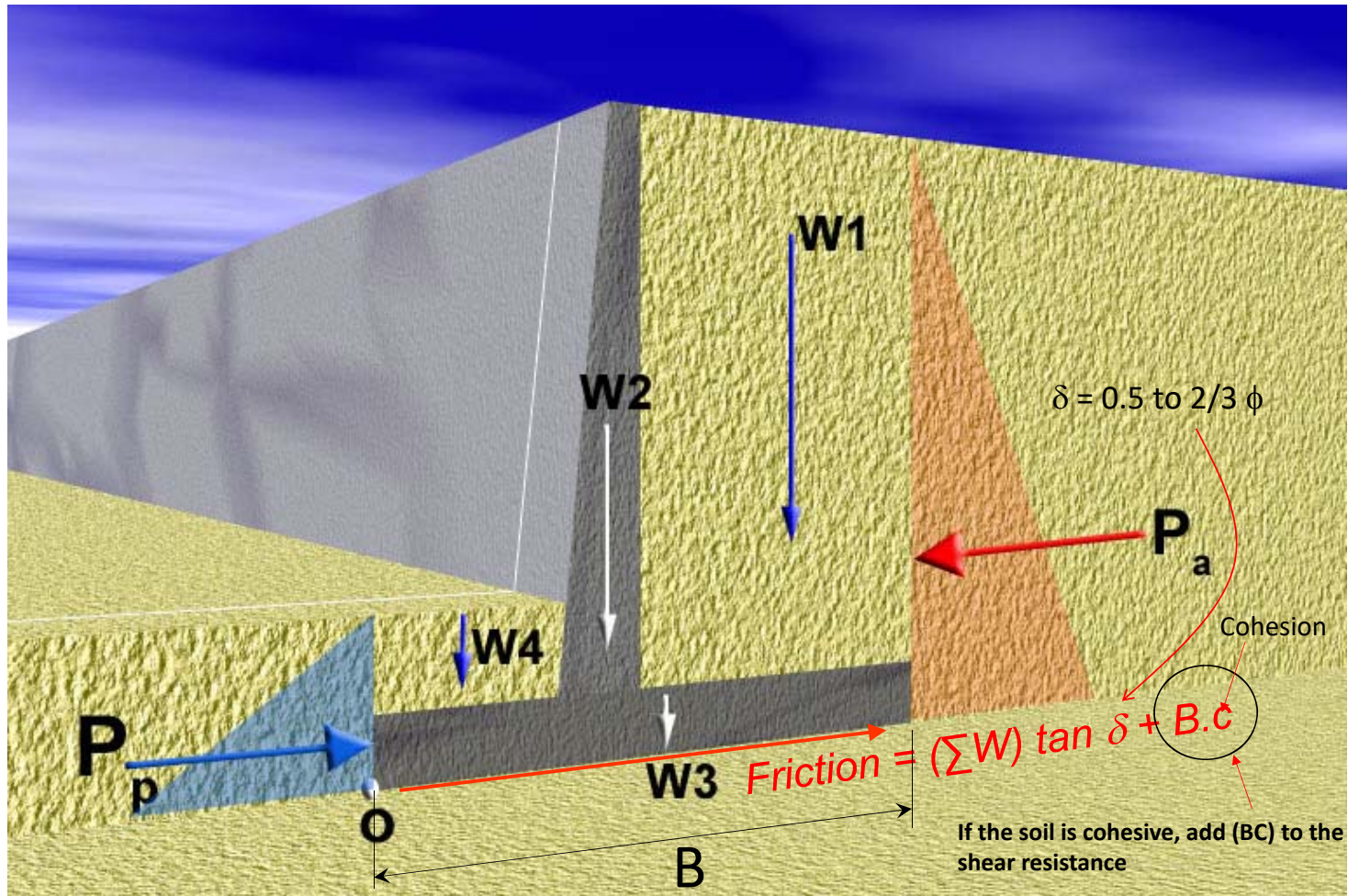


DETALLES DE MURO DE CONTENCIÓN

# I. External Stability

## 1- Sliding

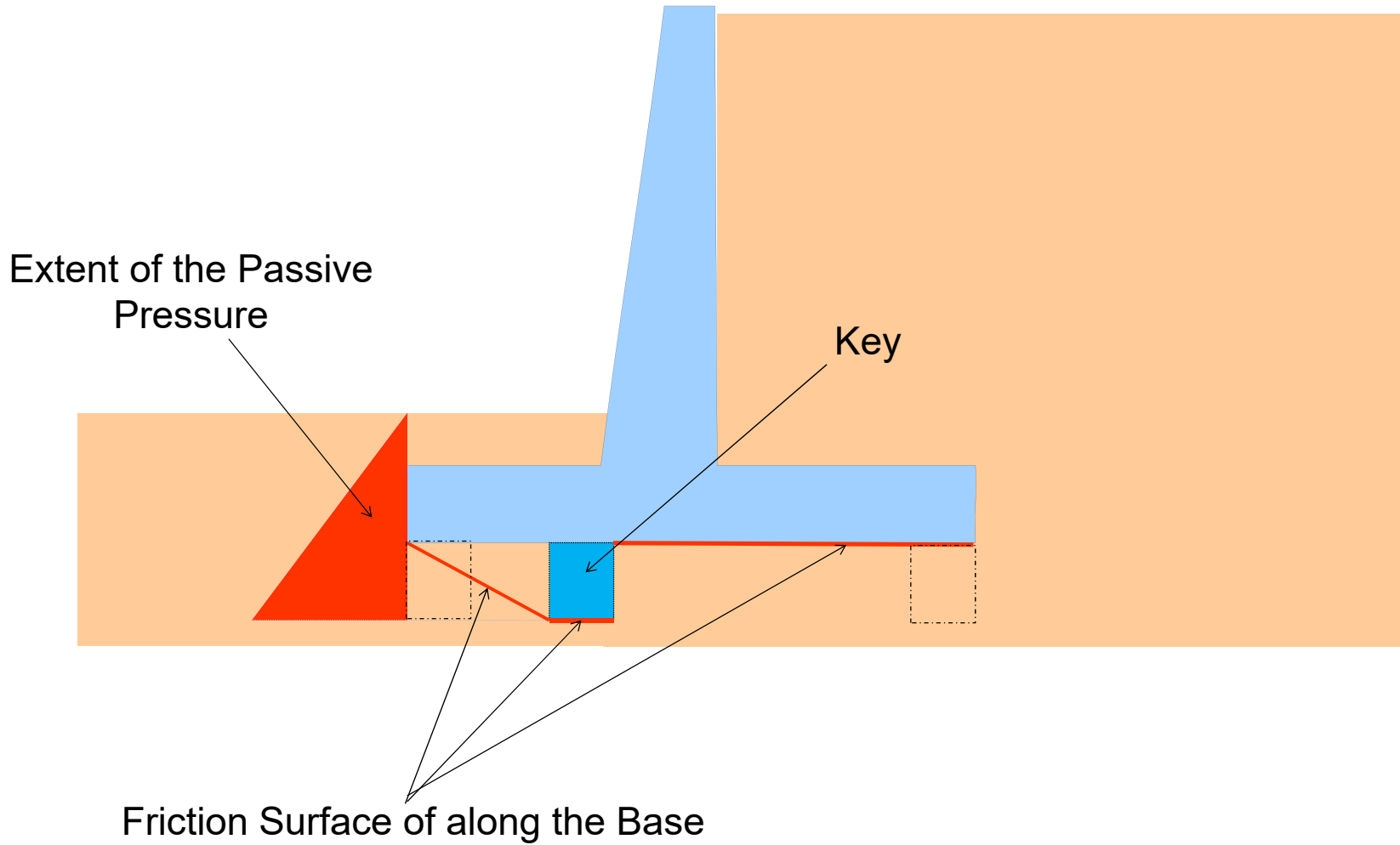
$$\text{Factor of Safety Against Sliding} = \frac{\text{Resisting Force}}{\text{Driving Force}} = \frac{F_R}{F_D}$$



$$F_D = P_a$$

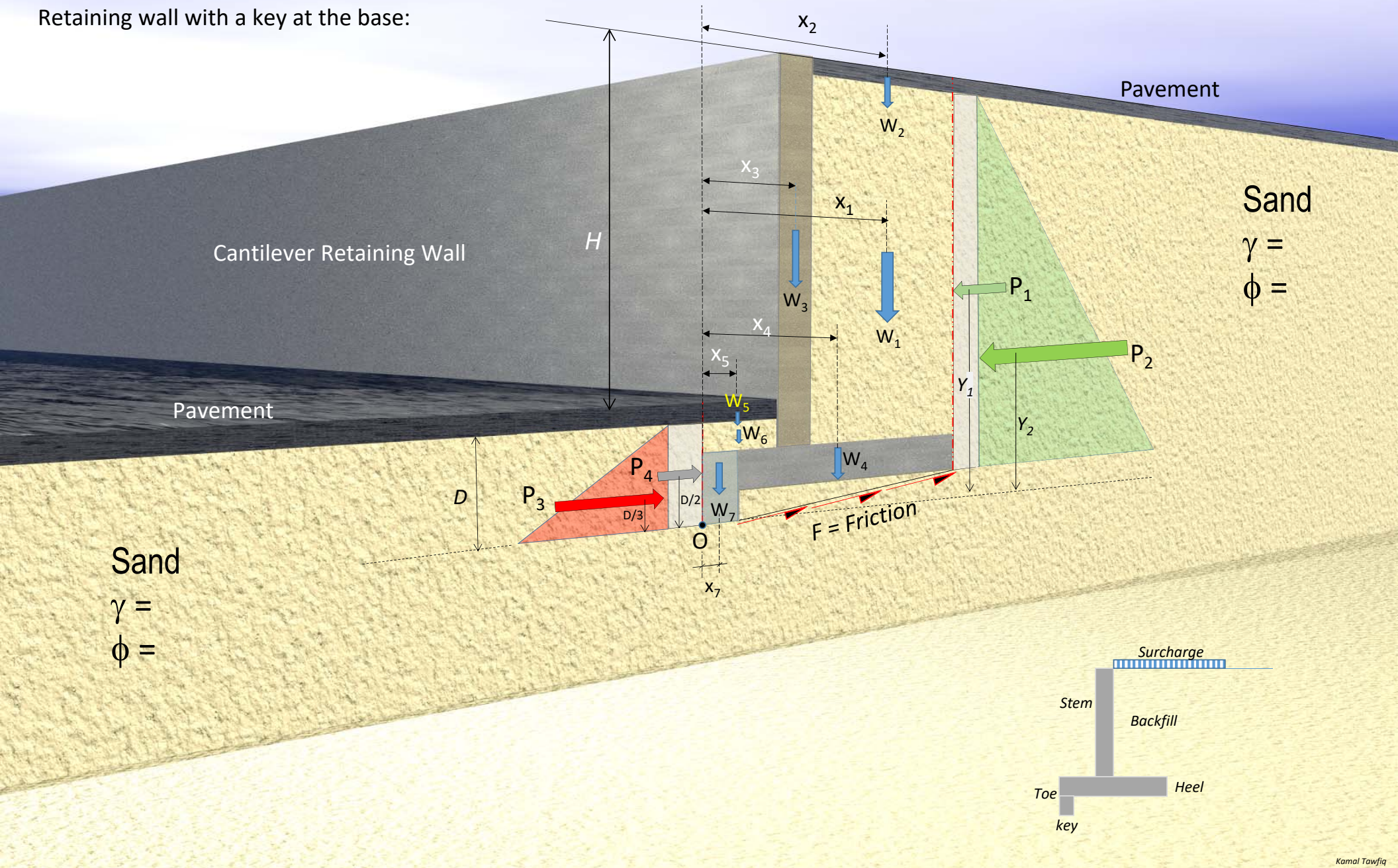
$$F_R = P_p + \text{Friction}$$

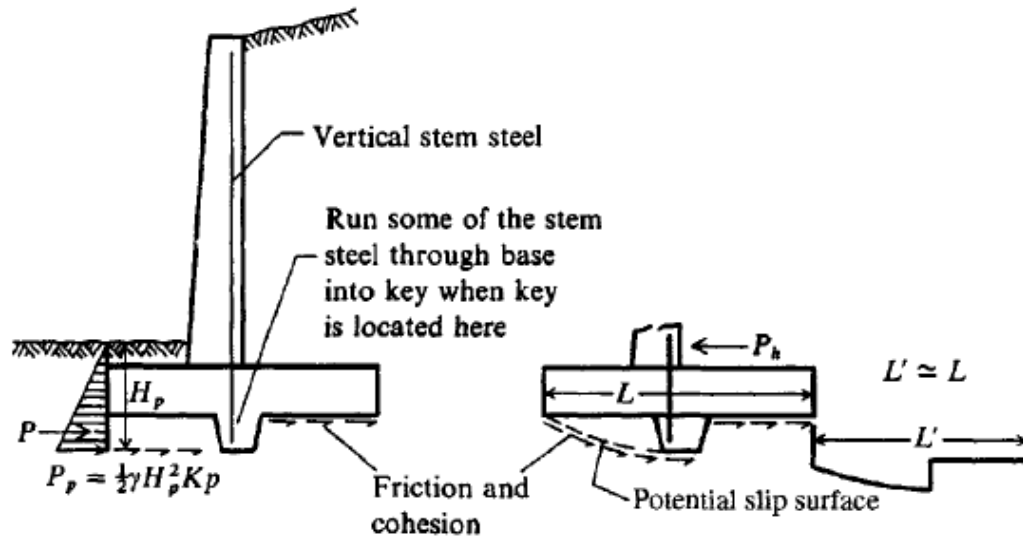
Using Key at the Base to Improve Sliding Resistance





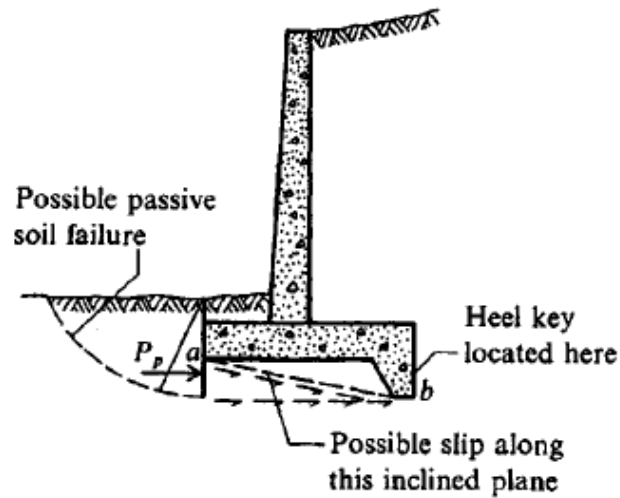
Retaining wall with a key at the base:





(a) Base key near stem so that stem steel may be extended into the key without additional splicing or using anchor bends.

(b) Potential sliding surface using the key location of *a*. There may be little increase in sliding resistance from this key, if the slip surface develops as shown.



(c) Possible sliding modes when using a heel key.

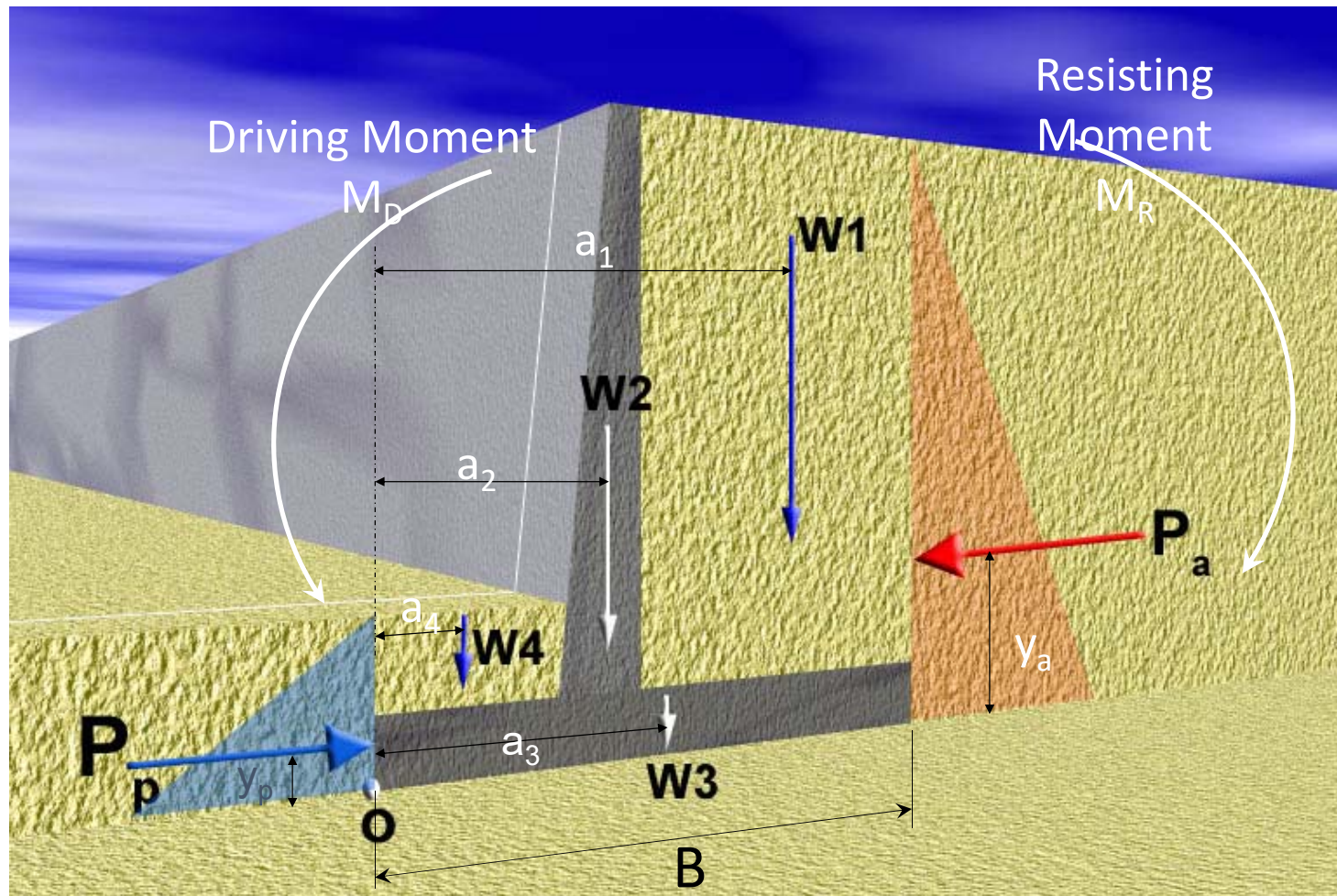
**Figure 12-14** Stability against sliding by using a base key.



# I. External Stability

## 2- Overturning

$$\text{Factor of Safety Against Sliding} = \frac{\text{Resisting Moment}}{\text{Driving Moment}} = \frac{M_R}{M_D}$$



Moment About o

$$M_D = P_a \cdot y_a$$

$$M_R = P_p \cdot y_p + W_1 a_1 + W_2 a_2 + W_3 a_3 + W_4 a_4$$



